

RESEARCH ARTICLE

Exploiting ecology in drug pulse sequences in favour of population reduction

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Abstract

A deterministic population dynamics model involving birth and death for a two-species system, comprising a wild-type and more resistant species competing via logistic growth, is subjected to two distinct stress environments designed to mimic those that would typically be induced by temporal variation in the concentration of a drug (antibiotic or chemotherapeutic) as it permeates through the population and is progressively degraded. Different treatment regimes, involving single or periodical doses, are evaluated in terms of the minimal population size (a measure of the extinction probability), and the population composition (a measure of the selection pressure for resistance or tolerance during the treatment). We show that there exist timescales over which the low-stress regime is as effective as the high-stress regime, due to the competition between the two species. For multiple periodic treatments, competition can ensure that the minimal population size is attained during the first pulse when the high-stress regime is short, which implies that a single short pulse can be more effective than a more protracted regime. Our results suggest that when the duration of the high-stress environment is restricted, a treatment with one or multiple shorter pulses can produce better outcomes than a single long treatment. If ecological competition is to be exploited for treatments, it is crucial to determine these timescales, and estimate for the minimal population threshold that suffices for extinction. These parameters can be quantified by experiment.

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Author summary

The possibilities of lower antibiotic dosages and treatment times, as demanded by antibiotic stewardship programmes have been investigated with complex mathematical models to account for, for example, the presence of an immune host. At the same time, microbial experiments are getting better at mimicking real setups, such as those where the drug gradually permeates in and out of the region with the infectious population. Our work systematically discusses an extremely simple and thus conceptually easy model for an infectious two species system (one wild-type and one more resistant population), interacting

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via logistic growth, subject to low and high stress environments. In this model, well-defined timescales exist during which the low stress environment is as efficient in reducing the population as the high stress environment. We explain which temporal patterns of low and high stress, corresponding to sequences of drug treatments, lead to the best population reduction for a variety of durations of high stress within a constant long low stress environment. The complexity of the spectrum of best treatments merits further experimental investigation, which could help clarify the relevant timescales. This could then give useful feedback towards the more complex models of the medical community.

Introduction

Despite recent searches for new classes of antibiotics, based on efficient screening of uncultured bacteria (or genomes) [1, 2], the decline in the rate of development of new types of antibiotic classes since the 1960s, and the concurring increase in drug-resistant organisms, is disconcerting [3, 4]. Growing fears that the world may be re-entering the 'prebioticera' [5] has prompted the World Health Organisation to publish a global action plan in 2015.

This plan explicitly underlines the importance of optimising current treatment strategies. This encompasses, for example, avoidance of the unwarranted prescription of antibiotics [6], since their use confers a selective advantage on the resistant variant. Practices include the use of redundant broad-spectrum antibiotics, or longer treatment durations than required to eliminate the infection [7, 8]. The optimal duration and intensity of treatments, with antibiotics or drugs in general, are subjects of controversial debates, particularly for cases where one already expects a mutant to be present initially [9, 10]. Of course, the ideal treatment should resolve the tension between reducing the advantage enjoyed by the resistant bacteria by preserving the other bacteria in the biomeDbest achieved by short, mild or specific application of antibiotics and conclusively eliminating the infectionDbest attained by long-term application of high doses of antibiotics of assured effect [11].

In this work, we compare antibiotic treatments, which we refer to as pulses or pulse sequences, with respect to their efficiency in reducing the population size of an infectious two-species population, consisting of one wild-type and one more resistant species. In our model, treatments with the same concentration profile and treatment length, but different numbers of pulses, are compared with each other, e.g. two shorter pulses compared to one longer one. A pulse sequence imposes different patterns of high or low stress on the bacteria, mimicking the gradual infiltration of the infection site and the slow degradation of the drug. Such environmental changes between high and low stress environments have previously been studied in the context of phenotypically heterogeneous populations [12]. Much theoretical work has investigated whether and how phenotypic switching can optimise the long-term fitness of the species under periodic or stochastic environmental variation [13–18]. We focus on reducing the size of a population in which the phenotypic switching rates are irrelevant apart from determining the initial composition of the population prior to treatment.

Exploiting competition between species to reduce the evolution of resistance?

To quantify pulse efficiency, we primarily study the minimal population size n_{\min} of our two-species system as a proxy for the extinction probability of the population. Antibiotic stewardship programmes suggest that for some diseases, such as pneumonia, the immune system can clear the residual infection once the bacterial population size is sufficiently reduced [19, 20].

Thus, the minimal population size may be a more relevant parameter than the exact extinction probability itself. Additionally, the general behaviour of the deterministic system and its observable n_{\min} is more robust than the extinction probability in the stochastic model, as in the latter, the precise form of stochastic noise, or the system size, would be important. The total population minimum n_{\min} can still serve to gauge the latter, which scales as $\exp(n_{\min})$ [21].

Before introducing our model in detail, we jump ahead and summarise the essential result of our work in Fig 1, which we discuss later in more detail. Fig 1 shows the value of the minimal total population size in the configuration space of drug concentration profiles, spanned by the width of the pulse (or duration of its high stress environment) on the x-axis and the form of the pulse on the y-axis, which will be explained later. Practically, these two properties of a pulse—its high stress duration and its form—are likely constrained: a very long duration of the high stress environment or stronger drug might be detrimental for patients due to, for example, a destructive impact on the gut microbiome [22, 23]. Similarly, some pulse forms, such as those where the highest possible drug concentration suddenly drops to zero at the pathogen location at the end of the pulse (here denoted by temporal skewness $s = 1$), may not be realistic for clinical treatments. However, since we do not want to make any assumptions on which parts of the configuration space should be accessible, we examine our system for all possible combinations of pulse form and durations of the high stress environments.

The colour code (symbols) signifies which of the four possible pulse sequences sketched on the right of Fig 1 most effectively reduces the population size. Fig 1 clearly shows that in our simple model setup, different pulse sequences are favourable in different regions of configuration space. The aim of this work is to outline phenomenologically which pulse sequence yields the lowest minimal population for which part of configuration space in Fig 1, and might therefore be most likely to drive the species to extinction. The best pulse sequence at any one point of Fig 1 tends to be the one that maximally exploits the competition between the more resistant and wild-type species, represented by logistic growth in our model. The simplicity of our approach makes explicit why some references might argue for more moderate treatments involving e. g. shorter or lower drug concentrations, but also what the limitation of models and observables are and hence why such moderate treatments may not work in real setups. We also examine how the population composition (a measure of how strongly the more resistant species dominates the population) evolves, should such a pulse sequence not lead to achieving extinction. Finally, we highlight the need for microbial experiments in such temporally varying drug gradients, in order to evaluate the applicability of simple models to real systems.

Materials and methods

Deterministic model for two-species birth-death process

The simplest model that can be used to study the effect of the temporal concentration profile on a heterogeneous population (n) consists of two phenotypically different species, a susceptible “wild type” species (w), and a more tolerant or resistant species (r). Its increased resistance comes at the cost of a reduced fitness in the drug-free environment, which is reflected in a smaller growth rate. As in previous works [24, 25], we assume that the drug is bacteriostatic, that is, it only affects growth, such that growth of each species ceases as soon as its minimum inhibitory concentration (MIC) is exceeded.

Thus, in this deterministic population dynamics model for the birth-death process, sketched in the inset of Fig 2, the growth rate of each species $\eta \in \{r, w\}$ is given by $\phi_{\eta}(t, n(t)) = \Theta[\text{MIC}_{\eta} - c(t)]\lambda_{\eta}(1 - n(t))$, where $n(t) = w(t) + r(t)$ is the total number of species at time t expressed in terms of a carrying capacity, which does not require specification as it serves

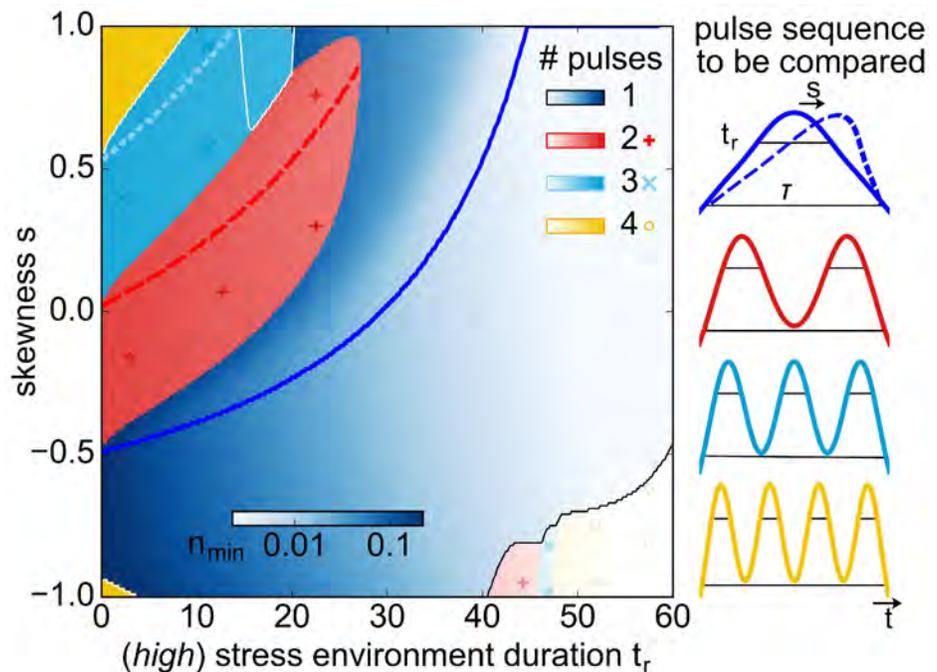


Fig 1. Comparison of the lowest population minimum n_{min} for drug treatment sequences of constant overall duration $\tau = 60$ providing the same total exposure to high stress t_r and low stress $\tau - t_r$ distributed over different numbers of identically-shaped pulses N . Parameters τ and t_r (x-axis), both given in units of growth rate, together with the skewness s , describing how t_r is positioned within τ , (y-axis), determine a drug pulse (sketched on the right). The colour code signifies the optimal N -pulse sequence for a certain choice of parameters t_r and s , and the shade indicates the value of the n_{min} . The coloured lines mark the skewnesses that give local minima for fixed t_r , corresponding to an optimal onset time for the respective number of pulses. In the non-blue regions a sequence of pulses is more effective than a single pulse, either because onset times are closer to the optimum value for higher number of pulses compared to one pulse (top left corner) or because the minimum n_{min} is reached in the last pulse of every sequence (bottom right corner; region surrounded by the black line).

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merely as a unit for the population size. The Heaviside-Theta step function Θ implies that the growth rate is only non-zero when the drug concentration is lower than the MIC of the corresponding species. The index $\eta \in \{r, w\}$ refers to the type of species (resistant or wild-type), and λ_η is its growth rate. The more resistant species has a lower basal growth rate in the drug-free environment, i.e., $\lambda_r = \lambda_w - k := \lambda - k$, where $k > 0$ can be interpreted as a cost that the resistant species incurs for being more resistant. The logistic growth assumed in this model introduces competition between the wild-type and the resistant species for limited space and/or resources, and places an upper bound on the population size. We also include a constant death rate δ for both species, meaning that a species decays at rate δ when $c(t) > MIC_\eta$. For these higher concentrations, growth of species η is inhibited and, since switching is negligible, the species can only die. All rates and times in this work are given in units of λ .

The time evolution of the population can be studied in terms of the differential equations

$$\begin{aligned} \dot{w}(t) &= [\phi_w(t, n(t)) - \delta - \mu_w]w(t) + \mu_r r(t) \\ \dot{r}(t) &= \mu_w w(t) + [\phi_r(t, n(t)) - \delta - \mu_r]r(t) \end{aligned} \tag{1}$$

since for sufficiently large populations stochastic fluctuations can be neglected. The two species are coupled via the competition from logistic growth, as well as via the switching rates

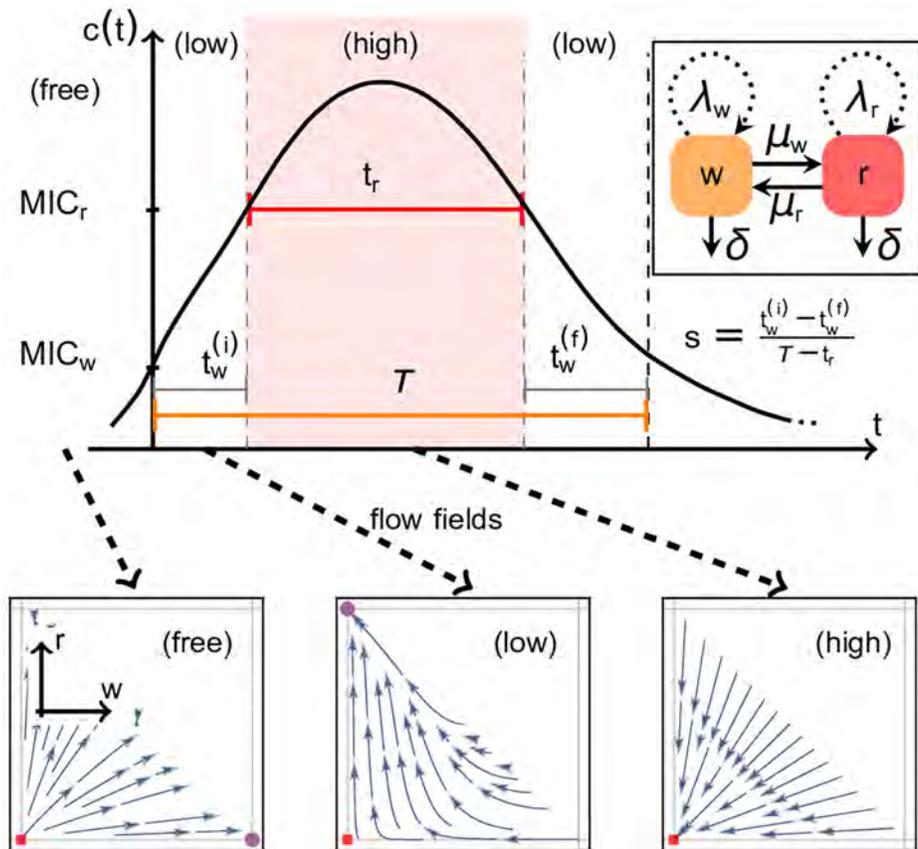


Fig 2. Top: Inset: Schematic of the two-species model: wild-type w and resistant r grow logistically at rates λ_w or λ_r , decay at rate δ and switch between states at rates μ_w or μ_r , respectively. Main figure: Time-dependent antibiotic pulse shape with the three parameters τ , t_r , and the skewness s as before. During t_r the antibiotic concentration $c(t) > MIC_r$ of the more resistant species (*high* environment), while during the entire treatment duration τ , $c(t) > MIC_w$ (*low* and *high* environment). Initially, the system is in the stress-free environment (*free*). Bottom: Dynamical landscapes in population phase space corresponding to these three different environments in antibiotic concentration: (*high*) environment, with one attractive fixed point (red dot) at $n = 0$; (*low*) environment, with a saddle point at $n = 0$ and an attractive fixed point on the r axis; (*free*) environment: with unstable fixed point at $n = 0$ and stable fixed point close to the w axis, $(w_{(free)}^*, r_{(free)}^*)$, which we use as the initial configuration.

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μ_w and μ_r . Phenotypically more resistant states can be characterised by a reduced growth rate, or complete growth arrest, often known as tolerance or persistence [26±28] (for a recent review, see Ref. [29]). Provided that $\mu_{w,r} \ll \delta$, which is the case for both mutation and phenotypic switching, our choice of $\mu_w = 10^{-6} \lambda$ and $\mu_r = 0$ does not qualitatively affect the results.

For this entire work, we used exemplary values of $\delta = 0.1\lambda$ and $k = 0.1\lambda$, where $\lambda \equiv 1$, i. e. we used λ as the basic unit of time. We investigate several other combinations of costs and death rates, in particular combinations with the same death rate, but a smaller and larger cost, in S1 Text. There, we show that our results and general statements are still valid for these cases. We chose the values of $\delta = 0.1$ and $k = 0.1$ since this combination allowed us to show the complete and most general picture of possible best pulse shapes in Fig 1. A smaller (yet also biologically possible) fitness cost would not have contained all different scenarios. We ask the reader to refer to S1 Text for more details.

Antibiotic pulse form determined by skewness and pulse width

Since in our model the only relevant information about the antibiotic concentration is whether it is above or below the MIC of the corresponding species, any pulse sequence is fully determined by the temporal arrangement of low-stress (*low*) and high-stress (*high*) environments. In these (*low*) and (*high*) environments, the antibiotic concentration is low, $\text{MIC}_w < c(t) < \text{MIC}_r$, or high, $c(t) > \text{MIC}_r$, respectively (sketched for a single pulse in the top panel of Fig 2). Before the pulse sequence, the system is in the drug-free environment (*free*), where the concentration of the antibiotic $c(t)$ is less than either MIC, $c(t) < \text{MIC}_{w,r}$. We assume that the (*free*) environment appears only before, but not during, a pulse sequence. Thus, the (*free*) environment determines the initial condition of the population, which we take to be at its fixed point, $(w(t=0), r(t=0)) = (w_{(free)}^*, r_{(free)}^*)$, shown as the purple dot near the w -axis of the phase space panel (*free*) of Fig 2.

The change in population size and composition in each of these environments is characterised by the flow field in phase space (w, r) , shown in the three lower panels of Fig 2. In the (*low*) environment, the population flows towards the more resistant species (high r and low w), while in the (*high*) environment, it flows towards the origin, meaning that both species die out exponentially.

Thus, the effect of a single pulse on the population crucially depends on the times spent by the system in the (*low*) and (*high*) environments. A single pulse involves a single (connected) environment of (*high*) antibiotic exposure, with (*low*) environment potentially preceding or succeeding this (*high*) environment. In reality, the duration of these (*low*) environments will depend on the experimental setup or host. A pulse sequence is composed of a succession of identical single pulses. We refer to the total time of the pulse as τ , and the time during which the system is in the (*high*) environment as t_r . The time periods during which the system is in the (*low*) environment (initially) before t_r and (finally) after t_r are denoted by $t_w^{(i)}$ and $t_w^{(f)}$, respectively. As this would overparameterise the pulse, we combine the latter two time scales into a skewness parameter $s = (t_w^{(i)} - t_w^{(f)}) / (\tau - t_r)$, signifying how t_r is positioned within τ . Skewness $s = -1$ ($s = 1$) thus denotes a pulse which starts (ends) with the (*high*) environment, while skewness $s = 0$ denotes a symmetric pulse.

Results

Minimal population

We compared pulse sequences of up to $N = 4$ pulses (same t_r and s) for constant treatment time τ for all possible skewnesses s and durations t_r . Thus, a single pulse with $\tau = 60$ and given t_r and s is compared with a sequence of N identical pulses, each defined by $\tau^{(N)} = 60/N$ and $t_r^{(N)} = t_r/N$ and s . (Further values of τ are discussed in S1 Text). The retention of the same skewness within a sequence is motivated by the fact that we assume that the rate of increase or decrease in concentration is primarily determined by the host system of the bacteria. In this comparison, the 'best' pulse sequence for given (t_r, s) is defined as the one that yields the lowest population minimum n_{\min} and so has the highest likelihood of eliminating the pathogen. In situations where the entire configuration space is accessible, the maximal t_r yields the overall lowest population minimum, independent of skewness s . Since practically the maximal duration t_r acceptable for treatments may be limited, it is important to know which pulse sequence is best for each (t_r, s) , such that we can provide intuition on any situation and parameter choice that may arise. The colour (and corresponding symbols) in Fig 1 show the best pulse sequences (i.e. the best N), and the shade indicates the value of n_{\min} (dark denotes high values).

We found that a single pulse is most effective over a large range of parameters (blue in Fig 1). In particular, for each duration in the (*high*) environment t_r , the lowest minimum across all skewnesses is obtained by a single pulse (blue line). This means that in practical situations which allow all different pulse skewnesses, a single pulse with a skewness on the blue line would give the lowest minimum. If, however, the possible pulse skewness is limited due to the host setup, a single pulse may not be the best choice. For ease of comparison, Fig 3 a shows n_{\min} for just a single pulse of constant treatment time $\tau = 60$, with the white line marking the lowest minimum (the blue line in Fig 1). In the next paragraph we focus on a single pulse in order to understand which pulse parameters (s , t_r) yield this lowest minimum.

Optimal $t_w^{(i)}$ determines lowest possible population minimum. We found that this lowest minimum always occurs for pulses with a constant initial time in the (*low*) environment, $t_w^{(i)}$, which we refer to as $t_o \equiv t_{w,\text{optimal}}^{(i)}$. Fig 3b±3d depict the behaviour of the total population in the (*low*) and (*high*) environment, with the (*high*) environment marked by the light red background. For a long $t_w^{(i)}$, i.e. a late onset of the (*high*) environment, the dynamics of the total population $n(t)$ (black) and the more resistant species $r(t)$ (red) are shown in Fig 3b. Initially $n(t)$ decays exponentially, as the dominating wild-type species dies off. Due to the competition for resources, modelled by logistic growth, r can grow appreciably only once w is sufficiently small. If $t_w^{(i)}$ is long enough, r grows up to the fixed point of the (*low*) environment (see flow in Fig 2). In order to avoid the regrowth of the population, which is then dominated by r , the (*high*) environment should be initiated at the time where r starts dominating and n is minimal (Fig 3c). This optimal $t_o \equiv t_{w,\text{optimal}}^{(i)}$ depends on the system parameters, and corresponds to $t_o \approx 15$ for our choice of parameters.

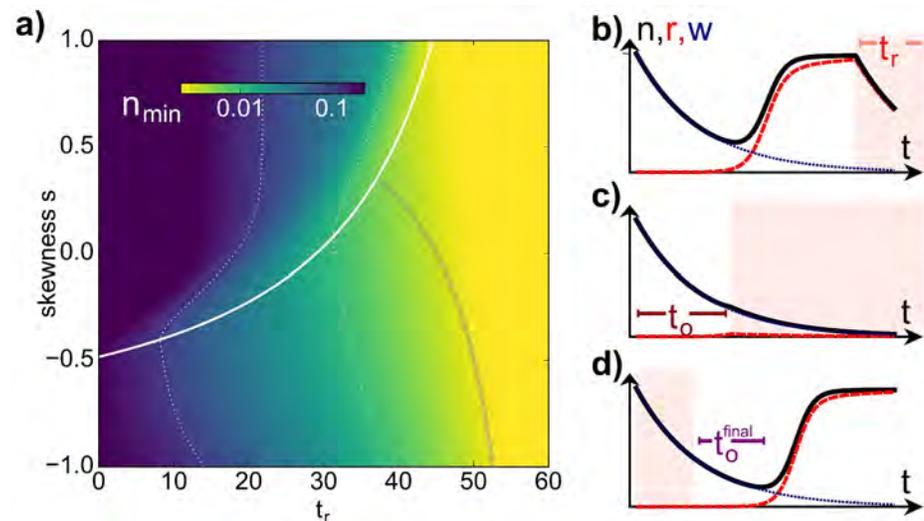


Fig 3. Which value of s gives the lowest population minimum for fixed t_r ? a) Lowest population minimum n_{\min} for a single pulse with constant $\tau = 60$ for all possible pulse shape parameters t_r and s . The optimal skewness $s_o = 2t_o/(\tau - t_r) - 1$ which gives the smallest n_{\min} for each t_r is marked in white, while the gray (dashed) line marks the skewness $1 - 2t_o^{\text{final}}/(\tau - t_r)$, where n_{\min} has dropped to its smallest value across t_r . The constant contours (dotted lines) serve as guides to the eye. b-d) Explaining t_o (c, cf. b) and t_o^{final} (d), the timescales for which the (*high*) environment is not more effective than the (*low*) environment. In b) $t_w^{(i)}$ is longer than t_o : the population (black) starts growing during the (*low*) environment, even though the wild type (blue dotted) decays, as the more resistant species (red) is not affected by the antibiotic. In c), $t_w^{(i)} = t_o$ and so the total population keeps decaying. d) If $t_w^{(i)} = t_o^{\text{final}}$ and the pulse ends there, a minimal n is achieved, while for $t_w^{(i)} > t_o^{\text{final}}$ n grows again.

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The population can also decay further after the (*high*) environment (Fig 3d). Analogously to $t_{w,optimal}^{(i)}$, there exists an optimal $t_o^{final} \equiv t_{w,optimal}^{(f)}$, marking the time after which r begins to dominate in the (*low*) environment at the end of the pulse. This then depends on t_r and $t_w^{(i)}$. The grey dashed line in Fig 3a marks the skewness corresponding to $t_o^{final}(t_w^{(i)} = 0)$ such that $t_o^{final} + t_r = \tau$. For negative s , this line indicates where n_{min} saturates as a function of t_r , such that a larger t_r does not yield any drastic changes in n_{min} . This means that due to the competitive growth, the (*high*) environment (t_r) can always be shorter than (*low*) environment (τ) while still having essentially the same effect as if $t_r = \tau$. A longer duration of (*high*) antibiotic stress is thus not necessarily more effective in reducing the bacterial population, while potentially being disadvantageous for the host.

For a survey of the dependence of both t_o and t_o^{final} on the system parameters, please refer to S1 Text.

For pulse sequences, the global population minimum can occur during any pulse.

When comparing pulse sequences with different N (number of pulses), it is important to note that every pulse produces a local population minimum, and the global population minimum can occur during any of these pulses (see green cross in Fig 4a+4c). In the following, we outline heuristically during which pulse the global minimum is likely to occur, and thus which n_{min} (from which pulse) should be compared to the n_{min} from the single pulse, or the other sequences. In practice, predicting which pulse leads to the lowest minimum and hence the highest extinction probability may well be important for treatment: if a later pulse leads to a much larger population reduction than the first, longer treatments with antibiotics are probably beneficial, while if the opposite holds true, the continuation of the treatment may be superfluous or even deleterious.

The population minimum attained during a pulse depends both on the total population size n at the beginning of the pulse, and on the effective duration of population decay. Later pulses in a sequence can in principle have a lower starting population n than the initial pulse, if w has already decayed and r not yet grown substantially (see section Population Composition).

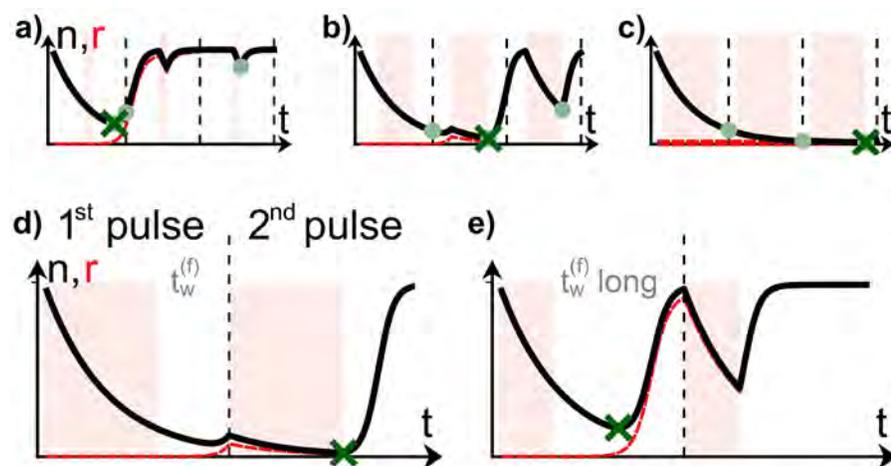


Fig 4. a-c) For a sequence of three pulses, the global population minimum can occur during any of the pulses, depending on the pulse parameters (a: $t_r = 6$, $s = 0$; b: $t_r = 30$, $s = 0$; c: $t_r = 45$, $s = -0.2$; $\tau = 60$ for all). The local minimum (within one pulse) is marked with a light green dot, the global minimum is marked with a green cross. In a, the value of n at the minima (green dots) increases successively, such that global minimum occurs during the first pulse. This is because $\tau - t_r$ is large. For b and c, $\tau - t_r$ decreases, implying that the global minimum shifts into the second and third pulse, respectively. Panels d-e show that for $s = -1$, the minimum is attained in the second pulse (d), unless $t_w^{(f)}$ is so long that the population can regrow to $n = r_{low}^*$ (e).

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However, the effective duration during which the population decays shortens from pulse to pulse, simply because w decreases: for example, we already saw that in a single pulse, the population can decay for $t_o + t_r$ or $t_o^{\text{final}} + t_r$ for $s = 1$ and $s = -1$. Both of these time periods of population decay are longer than t_r , the effective duration of decay in a pulse late in the sequence, where the population is entirely dominated by r .

Heuristically, the global minimum occurs during later pulses of the sequence for small $\tau - t_r$ (Fig 4c), corresponding to short periods per pulse spent in the (*low*) environment. This is because, in this case, the population n is small, as r cannot have grown drastically, and is additionally depleted during long stretches of t_r . Conversely, for small t_r (Fig 4a) the treatment is most efficient in the first pulse, as r progressively takes over the population in the (*low*) environment of each succeeding pulse. Thus, in the top left corner of Fig 1, we compare the minima from earlier pulses or the first pulse in each sequence, while in the bottom right corner, it is the later minima in the sequence that need to be compared.

For $t_r \ll \tau$ and high s , higher N pulse sequences do better, in fact already in the first pulse. With this in mind, we are now able to discuss the different features and regions of Fig 1.

First, we focus on the coloured sectors in the *top left corner* of Fig 1, corresponding to the region of parameter space where the best pulse sequence consists of two or three pulses. We found that in the part of the slice where the global minimum occurs in the first pulse (e.g. the red slice), the minimal population n_{min} can assume a minimum for each duration of the (*high*) environment t_r , similar to the blue line for the single pulse. This minimum arises because the initial (*low*) environment, with duration $t_w^{(i)}$, can be exploited to maximise population decay in longer pulse sequences as well. In order to know how long this (*low*) environment lasts for the first pulse of a longer sequence, we need to note that the first pulse in a two pulse sequence is only half as long as the full pulse for the single pulse. Thus, all relevant time scales need to be rescaled by N , i.e. the full pulse duration of a first pulse in a N -pulse sequence is $\tau^{(N)} = \tau/N$, the duration of the (*high*) environment is $t_r^{(N)} = t_r/N$, and the durations in the initial and final (*low*) environment are $t_w^{(i/f),(N)} = t_w^{(i/f)}/N$, where $t_w^{(i/f),(N)}$ denotes the time $t_w^{(i/f)}$ in one pulse of a N -pulse sequence. Then, the skewness at these minima for fixed t_r , marked by the red (dashed) and light-blue (dotted) lines in Fig 1, is given by $s_o^{(N)} = 2Nt_o/(\tau - t_r) - 1$ for N pulses. As a result of this multiplication by N compared to the optimal skewnesses for a single pulse, the lines marking the lowest population minimum within a region are shifted upwards for higher N sequences. (We remark on the side that the reason for why the red region does not extend all the way up to $s = 1$ is that a single pulse with a long $t_r^{(1)} > t_o + t_r^{(1)}$ will yield a lower n_{min} just by decreasing r (because the single pulse makes the population decay for at least t_r , whereas the initial pulse in the N -pulse sequence only decreases the population for $t_o + t_r^{(N)} = t_o + t_r/N$). This also applies to higher $\tau > 60$, such as shown in the S1 Text).

In the *bottom right corner* of Fig 1, marked with a thin black line, the last pulse in the sequence yields the lowest minimum. This region is located at negative s , indicating that now the time spent in the final (*low*) environment, $t_w^{(f),(N)}$, is important. Indeed, this can be seen clearly by considering a sequence of two pulses with $s = -1$, such as sketched in Fig 4d and 4e: the lack of an initial (*low*) environment *can* mean that a second pulse is better, because the population could in principle decay for a consistent run of the (*high*) and (*low*) environments of the first pulse, and (*high*) environment of the second pulse, which together corresponds to a time of $t_r^{(N)} + t_w^{(f),(N)} + t_r^{(N)}$ (Fig 4d). Indeed, for the second minimum not to be lower, the time in the (*low*) environment at the end of a pulse of the N -pulse sequence, $t_w^{(f),(N)}$, needs to be long enough for r to have grown up to $r_{(low)}^*$ before the onset of the second (*high*) environment of duration $t_r^{(N)}$ (Fig 4e). We note that such a long effective time of population

decay is not possible for $s = 1$, where the second pulse would begin with a second (*low*) environment, during which r can regrow. A more detailed argument, with an estimate for the t_r at which the second pulse provides a lower minimum (i.e. the beginning of the thin black line), is given in [S1 Text](#). For increasing t_r , the lowest minimum shifts to even higher N , so pulse sequences with increasing N perform better. In addition, the regime where $N > 1$ pulse sequences yield lower minima increases along the s -axis, until at $t_r = \tau$ all pulse sequences correspond to the same pulse and the minimum is equal across all skewnesses.

[Fig 1](#) also shows regions marked with a white line, where the lowest minimum occurs in an intermediate pulse in the sequence. We do not discuss this further here, but note for completeness that had we included longer pulse sequences, these regions would have split up further and shown that longer pulse sequences would give even lower minima in an intermediate pulse. For a better overview of the behaviour of regions where an intermediate pulse does best, we refer to Figs A and B in [S1 Text](#). The exact position of this region varies, if higher N pulse sequences are included, for different choices of fitness costs, death rate, and switching rate, and for different τ . Thus, a detailed analysis is not worthwhile, especially as the differences in the numerical values between the lowest minimum of a higher N -sequence, and the first minimum of a shorter sequence, are at least two magnitudes lower than the absolute value of n_{\min} there.

Population composition

In the previous section, we learnt which pulse sequences yield the maximal relative reduction in population size for which regions in (t_r, s) -space. This minimal population n_{\min} served as a proxy for gauging when extinction would most likely occur in a setting where an immune response can destroy the population when it is already small. Now, we would like to address a complementary question: in the event that extinction does not occur, whether because n_{\min} was too high, or the population was small for too short, what is the effect of such a 'failed' pulse on the bacterial population? We already saw that the composition of the population shifts more towards r with each pulse. In terms of real treatments, it might often be better not to pursue treatments which, if unsuccessful, entail a high risk of creating a fully resistant population. In order to evaluate the pulsed treatments associated with the most effective population reductions based on [Fig 1](#), we now focus on the population composition, quantified by the ratio of resistant to wild-type species, r/w , at the end of the best pulse within the best sequence. Evaluating r/w at the end of the pulse that yields the global minimum is motivated by the fact that the treatment can be stopped after, but not during, an individual pulse. [Fig 5b](#) shows the dependence of r/w on the pulse configuration, which can be best understood by first considering how the population evolves in (w, r) phase space during the different pulse sequences.

In [Fig 5a](#), we show trajectories for three pulse sequences, consisting of a single, two, or three pulses respectively, with $\tau = 60$ and $t_r = 10$. The qualitative behaviour of the phase space trajectory is independent of skewness (in [Fig 5a](#), $s = 0.9$, the corresponding trajectories for $s = -0.5$, $s = 0.2$ and $s = 0.5$ can be found in [Fig D](#) in [S1 Text](#)). The colour of the trajectory darkens progressively with every pulse in the sequence. The trajectory starts at the (*free*) fixed point close to the w -axis beyond the limits of [Fig 5a](#), and evolves towards the r -axis. Within each sequence, r/w steadily increases from pulse to pulse, as r progressively takes over the population during the (*low*) regimes. Thus, in the top left corner of [Fig 5b](#), where the first pulse of the sequence yields the lowest minimum, r/w is comparatively smaller (lighter shading). Indeed, the higher the N of the best sequence, the lower the ratio in [Fig 5b](#), provided the global minimum is reached in the first pulse (such as in the red region in [Fig 1](#)). The region marked with the white line in [Fig 1](#), where intermediate pulses (and not the first pulse) in the sequence yielded the

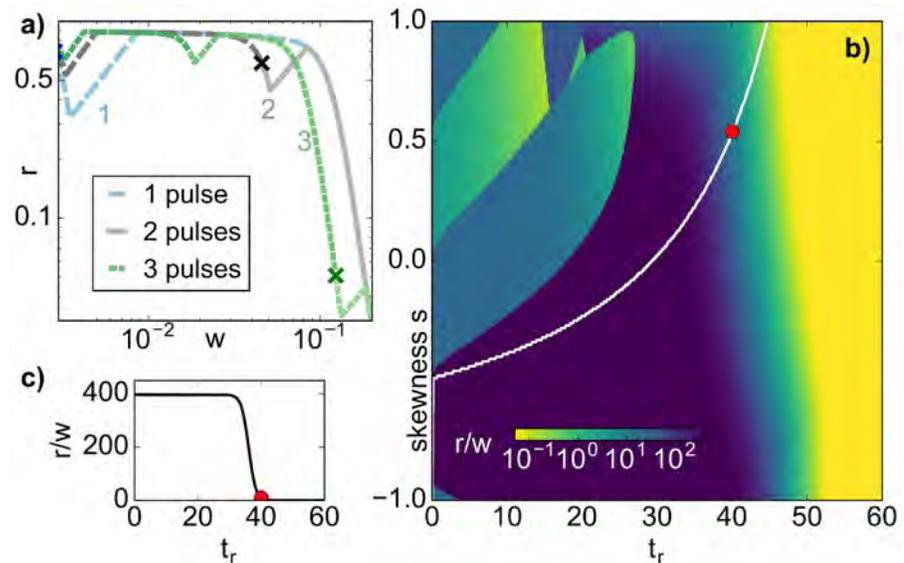


Fig 5. Panel a) Phase space (w, r) trajectories for parameters $\tau = 60$, $t_r = 10$, $s = 0.9$ and different numbers of pulses. The trajectories start from the fixed point of the antibiotic-free environment $(w_{(free)}^*, r_{(free)}^*)$, with r/w increasing with every pulse. Here, the sequence with three pulses gives the lowest minimum [see also Fig 1]. The cross marks the end of the best pulse within each sequence. Panel b) Ratio r/w at the end of the best pulse of the best sequence from Fig 1. For fixed t_r , r/w is best (smallest) in the regions where the first pulse in a high N pulse sequence yields the lowest n_{min} (top left corner, also in Fig 1). Similarly to Fig 3, the white line marks the skewness corresponding to the lowest minimum for each t_r , with the absolute value of the ratio dropping drastically at the red dot, shown in c). Panel c) Dependence of r/w on t_r along the white line in b). The ratio is approximately constant for $t_r < 30$ and then suddenly drops to the same value that it would also show at $t_r = \tau$.

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lowest global minimum, also shows up clearly as darker in Fig 5b. Here, r has grown more than for a single pulse, as more pulses were applied before the population minimum was reached.

Thus, in our model, when both population reduction and composition are considered, pulse sequences where the minimum is attained in the first pulse are generally more effective than a single long pulse: maintaining the (*low*) regime in the first pulse for around t_o keeps r/w as well as n_{min} small. This argument suggests that treating with this first pulse only achieves the best result, and additionally comes with a shorter total treatment duration τ and a shorter t_r . We would like to note that even if the population does not die out during this short treatment, multiple pulses of this form could be added in order to give the immune system more opportunities to eliminate the infection. These additional pulses would not drastically change r/w compared to the composition obtained after the single long pulse of $\tau = 60$. This can be seen also in Fig 5a, where for all pulse sequences the population composition is similar at the end of the entire sequence.

Single pulse ratio for optimal skewness drastically drops to a low value at $t_r < \tau$.

Finally, we wish to make an observation concerning the population composition following a single pulse, which dominates Fig 5b. Focusing on the dependence of the minimal n_{min} on t_r (white lines in Figs 3 and 5b, blue line in Fig 1), we see that the population composition along this line drops drastically at a certain $t_r < \tau$, as shown in Fig 5c (marked with a red dot). This means that also in terms of keeping the resistant species at bay, it is not necessary to impose the (*high*) environment for the entire duration of the pulse sequence.

Caveat: Fixing total antibiotic load, rather than τ , might reduce dependence on pulse form. So far, we have considered a constant drug expose time τ , corresponding to the entire treatment duration, which is also the quantity minimised in antibiotic stewardship programs. Alternatively, it could be important for medical applications to compare different pulses which keep the total load of antibiotic applied constant. Since our model does not incorporate any information relating to the antibiotic concentration, this question cannot be adequately addressed. Nevertheless, to a first approximation, $\tau + \alpha t_r$ might be a meaningful proxy for this total load, where α quantifies how MIC_w relates to MIC_r : $\alpha = \frac{MIC_r - MIC_w}{MIC_w}$.

In order to gauge the effect of applying a constant drug load, we fixed $\alpha = 1$ for simplicity, and show both population minima and composition for constant $t_{sum} = \tau + t_r$ for a single pulse in [S1 Text](#). Suffice it to say here that both quantities depend primarily on t_r , and only weakly on the skewness of the pulse. This is due to the fact that for $s = 1$, a constant t_{sum} exploits the optimal $t_w^{(i)}$, while for $s = -1$, the optimal $t_w^{(f)}$ is used. Since these quantities are not very different for our choice of parameters, constant t_{sum} effectively means that even though the skewness is different, the pulse will involve approximately the same τ and t_r for $s = 1$ and $s = -1$. A definite conclusion as to the effect of the form of the pulse on population reduction and composition for fixed antibiotic load is not possible within the scope of this work, and would in any case require a different model.

Discussion

Experimental relevance

Experiments with microbes can help investigate minimal antibiotic dosages and treatment times in a well-controlled test tube setup, where the impact of certain treatments on the microbial species itself can be studied without interfering effects, for example from the immune system. Such microbial experiments have, for example, helped suggest drug combinations or treatment regimens which could retard the development of antibiotic resistance [30–33]. Increasingly, these experiments try to incorporate practically important aspects of heterogeneities in the environment [34], such as drug concentration gradients. These gradients can enhance the development of bacterial resistance relative to spatially homogeneous systems [24, 25, 35, 36], as the more resistant species can successfully compete with a faster growing, but more susceptible wild-type species. Not enhancing the selective advantage of the more resistant species, in the context of temporal heterogeneities in drug levels, including the duration, frequency and even the concentration profile during a single antibiotic pulse, as studied also in this work, is also important in real treatments [7, 37], and is thus within the limits of current experiments.

Our model makes two drastic simplifications compared to real microbial species. First, we study only two species, instead of a series of possible phenotypically or genotypically different species. Typically, the evolutionary pathway that leads to a fully resistant species involves a variety of intermediate mutants, even when the mutational paths are constrained [38]. Since the fitness benefit diminishes with each successive mutation in a series [39, 40], we assumed that the strongest effect is conferred by the first mutation, and neglected all higher order mutants. For phenotypic switches, it is reasonable to consider only two species, corresponding to, for example, the expression or repression of a protein [41, 42]. Thus, our model should be applicable to experimental systems, while in real patients, different types of tolerant or persister cells might be involved [43], or even interact [44].

The second simplification concerns how these two species are affected by the antibiotic. In our model, we assume that the antibiotic is bacteriostatic, i.e. only affects the growth of the

species [24, 25]. We also assume that the growth rate of each species falls abruptly to zero when the antibiotic concentration is higher than their respective minimum inhibitory concentration (MIC) (see e.g. [45]). The experimental situation is more complex: cessation of growth is not instantaneous, the space occupied by a dead cell may not immediately become available [42], and the general use of the MIC as an indicator for slow growth is questionable [46]. However, an abrupt change in growth rate at MIC has been verified experimentally for *E. coli* and chloramphenicol. [25]. Additionally, our analysis is based on large numbers rather than extinction events which would be model specific; thus, small changes in the model (such as reduced but non-zero growth rate) should still give qualitatively similar results.

Evaluating the effect of different pulse sequences should be possible within a microfluidics setup, where, for example, periodically fluctuating environments have already been investigated for *E. coli* and tetracycline [42]. We expect that one should be able to observe that the (*low*) environment of drug concentration can be exploited in order to increase extinction probability for a (*high*) environment that is present for as short as possible, with the treatment time being constant. How long this duration of the (*low*) environment is for best exploitation would be sensitive to the growth rate of the more resistant species, which for tetracycline could be generated using a specific promoter, namely the *agn43* promoter [42, 47, 48]. Just as shown in Fig 1, we expect higher *N* pulse sequences to do better when this duration is optimal for them, but not for the longer pulse. In addition, further study of *E. coli* in combination with other antibiotics and more resistant strains should also show this, in addition to being more realistic than our simple model.

Summary and outlook. We studied the effect of a temporal pattern of antibiotic exposure, modelled as alternating periods of high and low stress, on a two-species bacterial population. Our results imply that, in fighting bacterial infections, one can make use of the competition between more and less resistant species. We showed that it is not necessary to impose the high stress regime for the entire duration of the treatment in order to obtain the best possible population depletion and composition. In the context of real infections, where a slow increase or decay of the drug concentration in the environment might be inevitable, it can be reassuring to know that the transient (*low*) stress regime need not be deleterious, and can indeed be exploited. However, if the low stress environment is maintained for too long, with this time-scale depending on the fitness of the more resistant strain, the latter will start to grow and eventually dominate.

If the duration of the high stress environment must be minimised (for example, due to its negative impact on other species in the biome), our model suggests that it is beneficial to split the treatment into several individual pulses, such that the total time spent in the (*low*) environment is equally distributed among the pulses (and hence shorter per pulse in the sequence than during a single application). In addition, multiple short treatments tend to be more effective when the absolute time spent in the high stress environment needs to be short. For very long treatment times, on the other hand, a single long application is more efficient. We expect these main results to be robust against a variety of practically relevant changes in the model, such as a break between treatment times, or a decreasing cost in the growth rate for the more resistant species.

Current medical research argues that more moderate treatments may be beneficial, if mutants are already present in a host. The conventional view has tended to assume that long and aggressive treatments are best at eradicating the infection and reducing the probability of evolving resistance [9]. In order to address this problem of infections in a host, mathematical and computational models for immunocompetent host have been introduced [49], or it has been suggested that an absolute population threshold can be used as a measure for extinction [50]. Following the latter suggestion, we have tried in this work to gauge the effect of the

immune system by understanding how the population can be reduced, but not driven to absolute extinction. Within the limits of our model, our results might support the more moderate approach. Other research focusing on ecological competition between species of different levels of resistance [51, 52] gave similar insights: on the population level, long and aggressive treatments reduce the probability of generating mutants, while more moderate treatments can exploit the inter-species competition [51]. From a physical perspective, it would be interesting to see how this more moderate approach can be reconciled with the physics of small numbers: when extinction is a rare event, the more traditional view supporting aggressive treatments might well be favoured. Either way, in the light of this current debate [53], it is important to determine the relevant timescales of growth of the different species in presence or absence of the drug [54], and how the species are coupled, in order to make models more realistic.

In order to obtain estimates of such timescales, it is important to use the knowledge obtained from well-controlled microbial model experiments on bacterial populations both in isolated and host environments (such as, for example, *C. elegans* culture [55, 56]). These experiments provide an ideal set-up for addressing these bigger questions, as they permit both small and large numbers of species to be studied and the environmental conditions can be precisely monitored.

Supporting information

S1 Text. Contains analogous figures to Fig 1 for a variety of costs and different τ , and a detailed discussion of the possible values for t_o and t_o^{final} and which minimum within a sequence might be the lowest minimum. It includes phase trajectories for different values of skewness s , and a brief discussion of how n_{min} and the population composition would be affected if the the total antibiotic load $\tau + t_r$ is fixed.
(PDF)

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Writing ± review & editing: Marianne Bauer, Isabella R. Graf, Vudtiwat Ngampruetikorn, Greg J. Stephens, Erwin Frey.

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